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# The Atmospheric Circulation over the North Atlantic as Induced by the SST Field

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## ABSTRACT

Spectral analyses of the sea surface temperature (SST) in the Simple Ocean Data Analysis (SODA) reanalysis for the past half-century identify prominent and statistically significant interannual oscillations in two regions along the Gulf Stream front over the North Atlantic. A model of the atmospheric marine boundary layer coupled to a baroclinic quasigeostrophic model of the free atmosphere is then forced with the SST history from the SODA reanalysis. Two extreme states are found in the atmospheric simulations: 1) an eastward extension of the westerly jet associated with the front, which occurs mainly during boreal winter, and 2) a quiescent state of very weak flow found predominantly in the summer. This vacillation of the oceanic-front-induced jet in the model is found to exhibit periodicities similar to those identified in the observed Gulf Stream SST front itself. In addition, a close correspondence is found between interannual spectral peaks in the observed North Atlantic Oscillation (NAO) index and the SODA-induced oscillations in the atmospheric model. In particular, significant oscillatory modes with periods of 8.5, 4.2, and 2.8 yr are found in both observed and simulated indices and are shown to be highly synchronized and of similar energy in both time series. These oscillatory modes in the simulations are shown to be suppressed when either (i) the Gulf Stream front or (ii) its interannual oscillations are omitted from the SST field. Moreover, these modes also disappear when (iii) the SST front is spatially smoothed, thus confirming that they are indeed induced by the oceanic front.

## 1. Introduction

Interannual and interdecadal oscillations emerge above a red-noise spectrum in many instrumental and proxy records of climate from the North Atlantic and the continents bordering it—see, for example, Bjerknes (1964), Deser and Blackmon (1993), Dettinger et al. (1995), Plaut and Vautard (1994), Hurrell and van Loon (1997), Moron et al. (1998), Da Costa and Colin de Verdière (2002), Kushnir et al. (2002), Hurrell et al. (2003), Feliks et al.

(2010a), and many others. The extent to which these oscillations may be ocean forced is still controversial, first because of the lack of consensus in atmospheric general circulation model (GCM) studies with prescribed sea surface temperatures (e.g., Robertson et al. 2000; Kushnir et al. 2002; Manganella 2008) and second due to the substantial influence that midlatitude atmospheric perturbations exert on the underlying ocean (Frankignoul and Hasselman 1977).

More recently, Feliks et al. (2004, 2007, hereafter referred to as FGS04 and FGS07) have presented modeling evidence that sharp SST gradients associated with midlatitude ocean fronts, such as the Gulf Stream and the Kuroshio Extension, can exert a strong influence on the overlying atmosphere, as well as on its low-frequency variability. In particular, this type of SST front was shown to force an atmospheric jet above it that extends vertically throughout the troposphere, and the variations in frontal strength were shown to modulate the atmospheric jet's intensity. Since oceanic fronts have a width of about

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100 km or less, they are not resolved by conventional GCMs, which typically have grid sizes of 200 km or more. However, recent GCM simulations with a resolution of roughly 50 km by Minobe et al. (2008) have confirmed the findings of FGS04 and FGS07 in terms of the existence of the atmospheric jet. Still, such GCMs cannot yet be run for the extended times needed to ascertain the impact of the SST fronts on the atmospheric jet's interannual and interdecadal variability.

In a spectral analysis of several climate indices, Feliks et al. (2010a) found a prominent oscillatory mode with a 7–8-yr period in indices over the North Atlantic, the Eastern Mediterranean, and the Ethiopian Plateau. An energy analysis of the synchronization between the projections of this oscillatory mode on the different regions analyzed suggested that the 7–8-yr mode might originate in the North Atlantic Ocean. Indeed, an oscillation with this period has been reported in several other studies of North Atlantic climate (Rogers 1984; Hurrell 1995; Hurrell and van Loon 1997; Robertson 2001; Da Costa and Colin de Verdière 2002; Gámiz-Fortis et al. 2002; Paluš and Novotná 2004). Feliks et al. (2010a) also detected an oscillatory mode with an approximate 4-yr period in all of the above regions; this mode appeared again to be associated with the North Atlantic, as well as to the quasi-quadrennial oscillation in the El Niño–Southern Oscillation variability.

The purpose of this paper is to show that the high-resolution SST history for the 50-yr interval 1958–2007, produced by the Simple Ocean Data Assimilation (SODA) reanalysis (Carton and Giese 2008), (i) exhibits interannual to near-decadal oscillations in the Gulf Stream's frontal region and (ii) indicates that these oscillations are capable of influencing the atmosphere above it, as simulated by a model of intermediate complexity. A brief introduction to the SODA data and to our atmospheric model is given in section 2; the model consists of a marine atmospheric boundary layer (MABL) coupled to a baroclinic, quasigeostrophic (QG) model of the free atmosphere. We then analyze the SODA SST data in section 3 and the model's response to it in section 4, using multichannel singular spectrum analysis (MSSA) to identify interannual oscillations in each dataset. In section 5, we compare the observed NAO index and the simulated index. In section 6, we summarize the results.

## 2. Data and methods

### a. The Simple Ocean Data Assimilation dataset

The SODA reanalysis of ocean climate variability from Carton and Giese (2008), version 2.0.2–4, provides the monthly SST dataset used in this study over the 50-yr

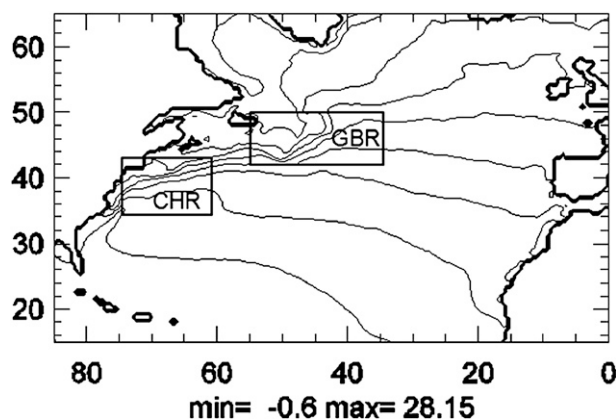


FIG. 1. Mean SST field in the North Atlantic over the curvilinear rectangle ( $15^{\circ}$ – $65^{\circ}$ N,  $85^{\circ}$ W– $0^{\circ}$ ) from SODA data over the 50-yr interval from January 1958 to December 2007. The heavy solid lines are the land boundaries, contour interval (CI) is 2.8 K, and extreme values (max and min) are given in the legend. Small rectangles indicate the two regions on which we concentrate in particular: 1) the Cape Hatteras region (CHR) ( $34^{\circ}$ – $43.50^{\circ}$ N,  $75^{\circ}$ – $60^{\circ}$ W) and 2) the Grand Banks region (GBR) ( $42^{\circ}$ – $50^{\circ}$ N,  $55^{\circ}$ – $35^{\circ}$ W).

interval 1958–2007, with a grid resolution of 0.5 degrees. The SST is taken to equal the temperature in the upper 5 m of the ocean. We also use the SODA sea surface height (SSH) field, which corresponds to the subsurface velocity, to aid us in the interpretation of the oscillations found in the SST field. The SODA is based on assimilating global ocean observations into an ocean GCM, originally developed at the NOAA Geophysical Fluid Dynamics Laboratory at Princeton, using the Parallel Ocean Program numerics (Smith et al. 1992): the observations include temperature and salinity profiles, additional hydrography, SSTs, and altimeter sea level data.

The annual mean SST field from SODA over the North Atlantic is shown in Fig. 1. The Gulf Stream front in SST is very prominent, with temperature changes of  $7\text{ K (100 km)}^{-1}$  across the front. The front is aligned with the Florida Current, which flows along the east coast of North America until the separation point at Cape Hatteras. A strong thermal front then extends into the open ocean to  $40^{\circ}$ W, beyond which it weakens abruptly and the isotherms diverge. The mean SSH field over the same area is shown in Fig. 2. The Gulf Stream front in SSH follows the SST front closely, with cross-frontal gradients reaching  $0.5\text{ m (100 km)}^{-1}$ ; this gradient corresponds to a subsurface current speed of about  $0.5\text{ m s}^{-1}$ .

### b. The atmospheric model

The atmospheric model has a marine atmospheric boundary layer (MABL), coupled to a quasigeostrophic (QG) baroclinic model of the free atmosphere. The

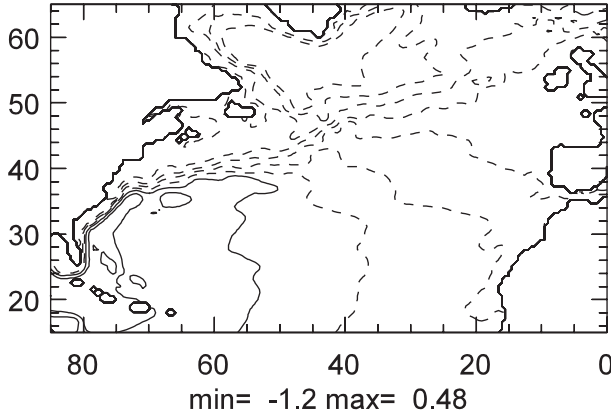


FIG. 2. Mean SSH in the North Atlantic over the same area as in Fig. 1 from the monthly mean SODA data. Solid (dashed) lines are positive (negative) differences from mean sea level, CI = 0.168 m.

MABL and QG models are described in detail by FGS04 and FGS07. For completeness, we provide here a summary of the main aspects of the model.

The frictional MABL model assumes a well-mixed moist boundary layer in equilibrium with the underlying SST field  $T = T(x, y)$ ; that is, the virtual potential temperature within the MABL is constant, while the flow in the free atmosphere above it is assumed to be geostrophic. The pressure gradient in the MABL has two components: one is due to the geostrophic wind in the free atmosphere at the top of the MABL and is independent of  $z$ ; this is the component familiar from boundary layer theory in all areas of geophysical fluid dynamics. The second component is due to the underlying thermal front and is a function of  $z$ .

The linear equations of motion in the MABL are

$$k \frac{\partial^2 u}{\partial z^2} + f v - \frac{1}{\rho} \frac{\partial p}{\partial x} = 0 \quad (1a)$$

and

$$k \frac{\partial^2 v}{\partial z^2} - f u - \frac{1}{\rho} \frac{\partial p}{\partial y} = 0, \quad (1b)$$

while the boundary conditions are

$$u = v = 0 \quad \text{at} \quad z = 0; \quad u = u_G, \quad v = v_G \quad \text{as} \quad z \rightarrow \infty. \quad (2)$$

The vertical wind profiles within the MABL can then be derived analytically in closed form, yielding the vertical

velocity  $w(H_E)$  at the top of the MABL by integrating the continuity equation:

$$w(H_E) = \frac{H_E}{2\pi} \left[ \zeta_G - \frac{g H_E}{f \theta_0} \left( 1 - \frac{1}{2\pi} \right) \nabla^2 T \right]. \quad (3)$$

Here,  $\zeta_G = \nabla^2 \psi$  is the geostrophic vorticity at the top of the MABL, while  $\psi$  is the geostrophic streamfunction. The MABL depth,  $H_E = \pi \sqrt{2k_0/f^2}$ , depends on latitude through the Coriolis parameter  $f$ , and  $k_0$  is a turbulent eddy coefficient. Numerical values of model parameters for the simulations of section 4 are given in Table 1.

The vertical velocity in (3) has two components: the first is associated with the geostrophic flow above the MABL, and we call it the mechanical component; the second is associated with the Laplacian  $\nabla^2 T$  of the SST, and we refer to it as the thermal component. The conventional Ekman pumping velocity given by the mechanical component is thus augmented here by a thermal component driven by  $\nabla^2 T$ . Note that while  $\zeta_g$  above the MABL is ultimately driven by  $\nabla^2 T$  since no other thermal forcing is included in the model, it is also a function of the dynamics of the free atmosphere, modeled here by using a QG baroclinic model. For our purposes, the analytical MABL model of FGS04 has advantages over the Lindzen and Nigam (1987) model, which was developed for the tropics, because ours is directly coupled to the free atmosphere's QG dynamics—the latter plays an important role in midlatitudes.

The baroclinic model of FGS07 consists of the standard QG potential vorticity equation (Pedlosky 1987; Holton 1992) with vertical decomposition in terms of the barotropic and first baroclinic normal modes following Flierl (1978) and Feliks and Ghil (1996). The equation for the modal amplitudes (Flierl 1978) is

$$\frac{\partial q_k}{\partial t} + \beta \frac{\partial \psi_k}{\partial x} + \sum_k \xi_{ijk} J(\psi_i, q_j) = r_H \nabla^4 \psi_k - \frac{H}{H_a} \phi_k(0) w_a(z=0), \quad (4)$$

where we only retain  $k = 0, 1$  and

$$q_k = \nabla^2 \psi_k - \lambda_k^2 \psi_k, \quad \xi_{ijk} = \int \phi_i \phi_j \phi_k dz. \quad (5)$$

TABLE 1. Characteristic scales and reference values for the atmospheric model.

$L$ (km)	$H$ (km)	$H_a$ (km)	$H_E$ (km)	$T_i$ (day)	$V$ (m s <sup>-1</sup> )	$\beta$ (m <sup>-1</sup> s <sup>-1</sup> )	$k_0$ (m <sup>2</sup> s <sup>-1</sup> )	$K_H$ (m <sup>2</sup> s <sup>-1</sup> )	$f$ (s <sup>-1</sup> )	$g$ (m s <sup>-2</sup> )	$\theta_0$ (K)	$\rho_0$ (g cm <sup>-3</sup> )	$L/\lambda_1$ (km)
50	10	10	0.8	0.58	1	$1.8 \times 10^{-11}$	3.3	$10^2$	$10^{-4}$	9.81	300	$10^{-3}$	575

The triple interaction coefficients  $\xi_{ijk}$  are all equal to zero or one except  $\xi_{111}$ ; we shall refer to the value of  $\xi_{111}$  by  $\xi$ .

Using (1) for  $w(H_E)$ , the lower-boundary condition for the free atmosphere at  $z = 0$  is

$$\frac{H}{H_a} \frac{d}{dt} \left[ \frac{\partial}{\partial z} \left( \frac{1}{S} \frac{\partial \psi}{\partial z} \right) \right] = \frac{H}{H_a} w_a(x, y, z = 0, t) = \gamma \nabla^2 \psi - \alpha \nabla^2 T \quad (6)$$

in which

$$\alpha = \frac{1}{2\pi} \left( 1 - \frac{1}{2\pi} \right) \frac{g H_E^2}{H_a V^2} \frac{T^*}{\theta_0} = \frac{1}{2\pi} \left( 1 - \frac{1}{2\pi} \right) \frac{H_E}{H_a} \frac{1}{F_r^2};$$

$$\gamma = \frac{1}{2\pi} \frac{H_E f L}{H_a V} = \frac{1}{2\pi \varepsilon} \frac{H_E}{H_a},$$

where  $H_a$  is the height of the free atmosphere,  $L$  is the horizontal length scale across the front,  $V$  scales the wind speed in the cross-front direction, and the (non-dimensional) temperature  $T$  scales like the oceanic frontal strength  $T^*$ . The constants  $\alpha$  and  $\gamma$  determine the relative importance of the coupling between the MABL and QG dynamics above. Note that  $\alpha \sim 1/\text{Fr}^2$  and  $\gamma \sim 1/\varepsilon$  and that both are proportional to  $H_E/H_a$ , where  $\text{Fr}$  is the Froude number,  $\varepsilon$  the Rossby number, and  $H_E/H_a$  is the ratio between the height of the MABL and that of the free atmosphere. Since  $\alpha$  is proportional to the strength  $T^*$  of the SST front, it is clear that stronger SST fronts induce stronger atmospheric circulations. A thicker MABL has a larger influence on the spinup by the SST front than on the spindown by the mechanical component since  $\alpha \sim H_E^2$  while  $\gamma \sim H_E$ .

The physical mechanism represented by the coupled MABL–QG model, by which the SST front influences the free atmosphere, is sketched in Fig. 3a. Two mechanisms combine to spin up the strong eastward jet. The first mechanism is based on a midlatitude stirring—from initial zero momentum—and it induces a strong, narrow eastward jet at the latitude of the stirring and a weak broad westward flow at other latitudes owing to the  $\beta$  effect. The strong jet is the result of keeping the net momentum zero (Salmon 1998, p. 277, Fig. 6.4), and its length is determined by the Rhines scale. This mechanism is prominent in the upper layers, as shown in Fig. 12 of section 4a, at an altitude of 10 km.

The second mechanism is a “breezelike” circulation induced by the sharp SST gradient across the front: this SST gradient causes a pressure gradient in the MABL that gives rise to a transverse ageostrophic circulation; the latter leads, via mass conservation, to a thermally induced pumping of the free atmosphere. This pumping then spins up a jet that runs parallel to the front, extends

through the depth of the free atmosphere, and is governed by QG dynamics, as shown by Feliks et al. (2010b). This mechanism is relevant to the lower layers since the breezelike circulation is found below 3 km, as seen in the surface layer of Fig. 12. As the SST front weakens, the thermal component of  $w(H_E)$  decreases and the mechanical components tend to spin the jet down. So we can expect the length of the jet in the upper layers to differ from that in the lower layers; our model simulation of section 4a confirms this difference—it appears, indeed, in Fig. 12.

No large-scale temperature gradients are imposed in the QG model, which thus represents only the atmospheric response to the SST-induced vertical velocity, rather than to equator–pole temperature differences. Nonetheless, this jet is in thermal wind balance and is both barotropically and baroclinically unstable, as discussed in FGS07. Snapshots of the thermal and mechanical components of  $w(H_E)$  are shown in Fig. 3b. The thermal component is larger by two orders of magnitude than the mechanical component above the oceanic front, so it gives rise to the strong atmospheric jet (see Fig. 12 below). In both components the large values follow the Gulf Stream front closely between Cape Hatteras and 42°W; farther to the east, the SST front weakens abruptly and so do both components of  $w(H_E)$ . The small-scale structures found in the mechanical component are due to the tendency of the enstrophy,  $(\nabla^2 \psi)^2$ , to cascade to the smaller scale in QG turbulence (Charney 1971).

The correspondence between two-mode and two-level models (Flierl 1978) is given by

$$H_1 = \frac{\left( \sqrt{\xi^2 + 4} - \xi \right)^2}{4 + \left( \sqrt{\xi^2 + 4} - \xi \right)^2}, \quad (7)$$

where  $H_1$  is the nondimensional upper-layer depth and  $H_2 = 1 - H_1$  is the lower-layer depth. For an interaction coefficient  $\xi = 0$ , we have  $H_1 = H_2 = 1/2$ , whereas large negative values of  $\xi$  give  $H_2 \sim \xi^{-2}$ . In the basic experiment of section 4, we take  $\xi = -1$ , which corresponds to the dimensional values  $H_1 H = 7230$  m and  $H_2 H = 2770$  m, given  $H = 10\,000$  m (see Table 1); values of  $\xi = -1$  or  $H_2:H_1 = 3/7$  are often used in atmospheric models (e.g., Kravtsov et al. 2005).

The streamfunction at any height  $z$  is given by

$$\psi(z) = \psi_{\text{BT}} + \phi_1(z) \psi_{\text{BC}}, \quad (8)$$

where  $\phi_1(z)$  is the vertical structure of the first baroclinic mode;  $\phi_1(0) = 2$  corresponds to the surface ( $z = 0$ ), that is, at the top of the MABL; and  $\phi_1(H) = -2$  corresponds to the top of the free atmosphere, that is, at an altitude of 10 km.



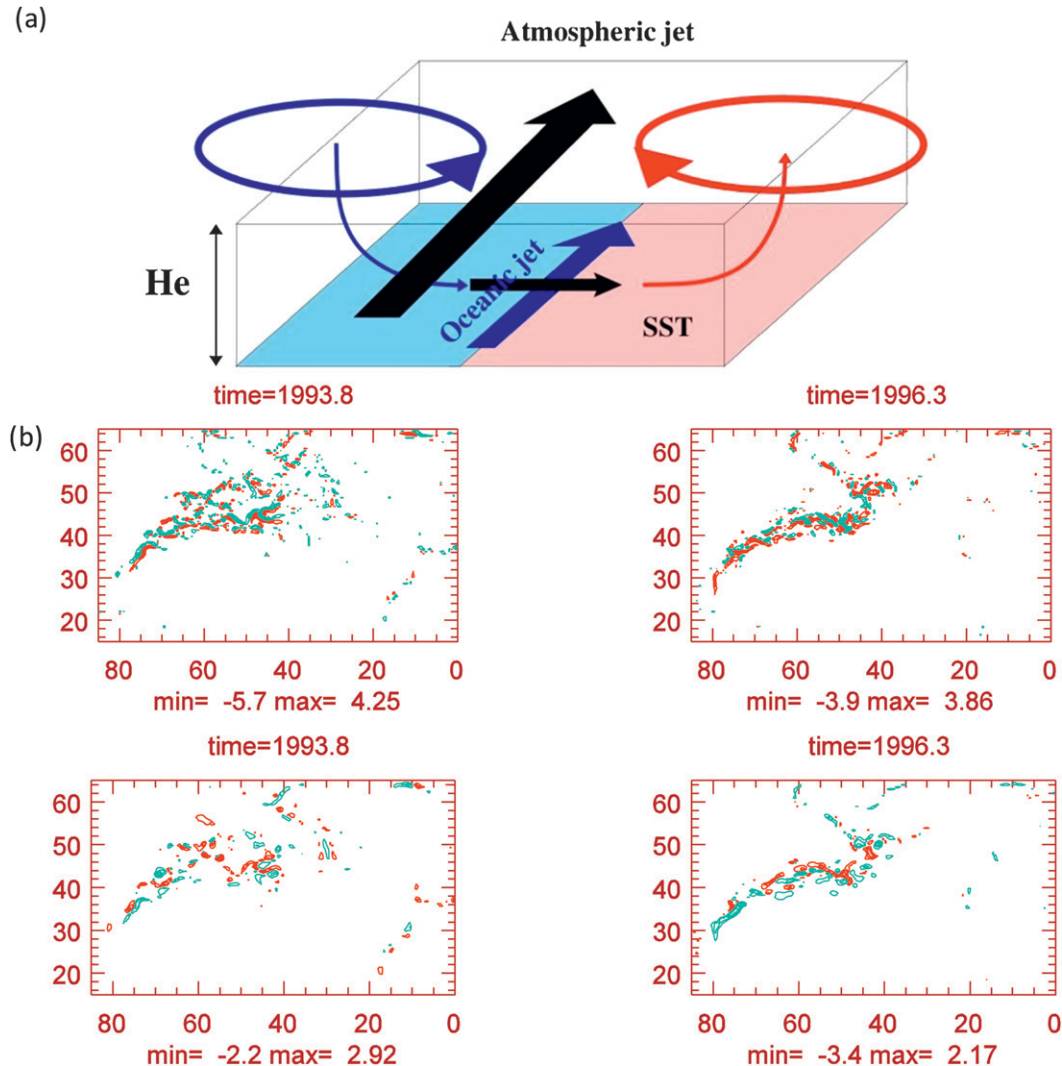


FIG. 3. (a) The mechanism for atmospheric jet generation proposed by FGS04: the oceanic jet (heavy blue arrow) gives rise to an atmospheric jet stream (black arrow above), accompanied by a double-gyre circulation (red and blue circles) up to the tropopause level; warm color indicates the warm side of the oceanic front. (b) Snapshots of the (top) thermal component  $\alpha \nabla^2 T$  of the vertical velocity  $w(H_E)$ , and of the (bottom) mechanical component  $\gamma \nabla^2 \psi$  in the North Atlantic over the area of Fig. 1. Red contours indicate upward velocity, that is, anticyclonic rotation in the horizontal.

Along the meridional boundaries, we impose free-slip conditions,  $\psi = q = 0$ , while in the zonal direction we use periodic boundary conditions with sponge layers in the  $\Delta L = 1000$  km adjacent to the boundaries. To examine the role of the width  $\Delta L$  of the sponge layer on the solution, we carried out two additional experiments with different widths,  $\Delta L = 750$  km and  $\Delta L = 500$  km; see section 4b.

The numerical scheme is the same as in Feliks (1990) and Feliks and Ghil (1996). Key features include fourth-order accurate discretization by finite elements in the horizontal (cf. Haidvogel et al. 1980) and a second-order Adams–Bashforth scheme in time. FGS04 showed that the correct generation of an atmospheric jet by the SST front requires a horizontal grid resolution of 50 km or

less, as confirmed by Minobe et al. (2008). At slightly lower resolution, FGS04 also indicated how to increase the nominal strength of the oceanic front in a self-consistent way so as to compensate for the loss of adequate resolution. FGS07 also studied the role of the two-layer depth ratio  $H_2:H_1$  on the evolution. They found that the baroclinic transients became more and more significant, though, as this ratio tends to 1; hence, all longer-term behavior, on the time scale of months, is mostly baroclinic.

### c. Spectral analysis methods

The primary methods of spectral analysis used here to identify oscillatory modes of variability in the SODA data and atmospheric model simulations are univariate

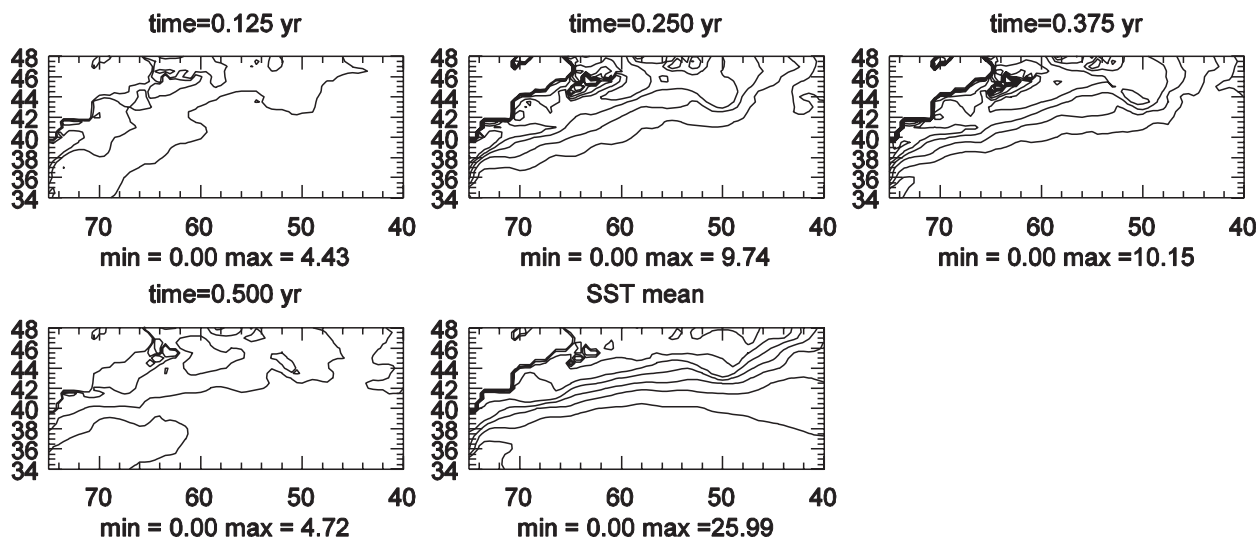


FIG. 4. Seasonal cycle of the SST field in the western North Atlantic ( $32^{\circ}$ – $48^{\circ}$ N,  $75^{\circ}$ – $40^{\circ}$ W) for the 50 years 1958–2007, with the year divided in eighths rather than months. Composites of the 1-yr mode, in four phase categories, correspond to one-half of the annual cycle, namely, June–November. Phases are labeled by the midpoint of the phase category. The panels look very similar for the other half of the cycle, December–May, only with opposite sign; that is, the spatial pattern in the panel for 0.625 yr (not shown)  $\approx$   $-($ panel for 0.125 yr $)$ , etc. These composites are based on the MSSA pair (1, 2), which captures 90% of the total variance (positive contours solid, negative ones dashed). CI = 1 K for these four panels, and CI = 1.7 K for the mean SST field (last panel).

singular spectral analysis (SSA) (Broomhead and King 1986a; Vautard and Ghil 1989; Ghil et al. 2002a) and multichannel SSA (MSSA). The MSSA is an extension of SSA to several time series, with each “channel” corresponding to one of the scalar time series of interest (Broomhead and King 1986b; Keppenne and Ghil 1993; Plaut and Vautard 1994; Ghil et al. 2002a). The method essentially diagonalizes the lag-covariance matrix associated with the vector time series whose components are the channels. The eigenvectors of this matrix are the space–time (ST) empirical orthogonal functions (EOFs), and the projection of the original data onto them yields the corresponding principal components (PCs).

MSSA is therewith a data-adaptive method of spectral analysis, whereby oscillatory components of variability—that may be modulated in phase and amplitude over time—are captured as pairs of eigenmodes with similar eigenvalues. A Monte Carlo (MC) statistical significance test against red noise is performed by comparing the projection of the data onto a given ST EOF for each channel with the corresponding projections of a large ensemble of red-noise surrogates. The power spectrum of this Monte Carlo SSA (MC MSSA) (Allen and Robertson 1996; Ghil et al. 2002a) method consists of an eigenvalue spectrum plotted against the dominant frequency associated with each eigenvalue  $k$ , estimated from the reduced Fourier transform of the associated PC time series (Vautard et al. 1992). The entire vector time series, or parts thereof that correspond to trends,

oscillatory modes, or noise, can be reconstructed by using linear combinations of these PCs and ST EOFs, yielding spatiotemporal reconstructed components (RCs).

### 3. Spectral analysis of SODA data

To examine the impact of the Gulf Stream front on the atmosphere we first analyze the frequency spectra of SST and SSH along the Gulf Stream track, performing the analysis in two rectangular regions where the inter-annual oscillations of  $\nabla^2 T$  exhibit their largest values. These two regions correspond to 1) the Cape Hatteras region (CHR:  $34^{\circ}$ – $43.50^{\circ}$ N,  $75^{\circ}$ – $60^{\circ}$ W) where the Gulf Stream front associated with the subtropical gyre separates from the coast and 2) the Grand Banks region (GBR:  $42^{\circ}$ – $50^{\circ}$ N,  $55^{\circ}$ – $35^{\circ}$ W) where the Gulf Stream front diverges abruptly due to the confluence between the subtropical and subpolar gyres. The two regions are outlined in Fig. 1.

We first apply MSSA to the SST data over the entire North Atlantic domain with a window width  $M = 150$  months. The leading pair of ST EOFs 1 and 2 captures the strongest oscillatory mode; it has a period of 1 yr, contains 90% of the variance, and represents the very strong seasonal cycle in SSTs. Phase composites of the corresponding reconstructed components, denoted by RCs (1, 2), are shown in Fig. 4, where the cycle has been divided into eight phase categories using the methodology of Moron et al. (1998).

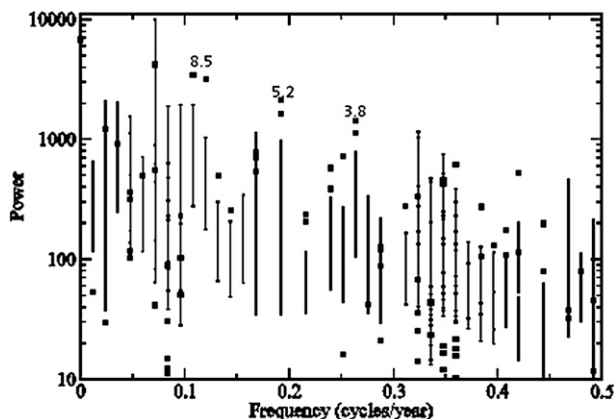


FIG. 5. Spectral analysis of the SST evolution in the CHR region ( $34^{\circ}$ – $43.50^{\circ}$ N,  $75^{\circ}$ – $60^{\circ}$ W), using Monte Carlo (MC) MSSA with a window width  $M = 150$  months, after subtracting the seasonal cycle. The estimated variance of each mode in the dataset is shown as a filled black square, while lower and upper ticks on the error bars indicate the 5th and 95th percentiles of a red-noise process constructed from a surrogate data ensemble of 100 time series. Each of the surrogates has the same variance and lag-one autocorrelation as the original record. The surrogate time series (Allen and Smith 1996) were produced by projecting the first 10 principal components of the MSSA analysis onto the basis vectors of a red-noise process. Highly significant pairs are labeled by their period.

The seasonal changes are strongest north of the front, with a peak amplitude of almost 10 K. The seasonal movement of the SST front is most prominent between  $35^{\circ}$  and  $40^{\circ}$ N along the coast and on the continental shelf downstream from Cape Hatteras; the separation point of the front moves quite visibly northward during the summer. The SST gradient across the front decreases during summer and increases during winter. Thus, we expect a strong atmospheric jet during the winter and weak flow during the summer, as will be seen in Fig. 12.

To isolate interannual oscillations in the CHR and GBR regions, we first filtered out the annual cycle and subannual variability by applying a 12-month running average to the dataset: doing so is preferable to the simple use of annual means—compare to Feliks et al. (2010a). Next, we applied MSSA to the prefiltered data in each region separately, with a window width of  $M = 150$  months. Only those signals significant at the (two-sided) 95% level will be analyzed further below.

The MSSA spectrum of the field SST in CHR is shown in Fig. 5 together with error bars that indicate the 95% confidence interval for a red-noise process. Oscillations with periods of  $\sim 8.5$ , 5.2, and 3.8 yr emerge as statistically significant and will be analyzed below. The leading oscillatory mode, captured by ST EOFs (3, 4), has a period of  $\sim 8.5$  yr and contains 13% of the interannual variance. The sum of the two RCs of this oscillatory mode, RC (3, 4), is shown in Fig. 6 at the point ( $37^{\circ}$ N,

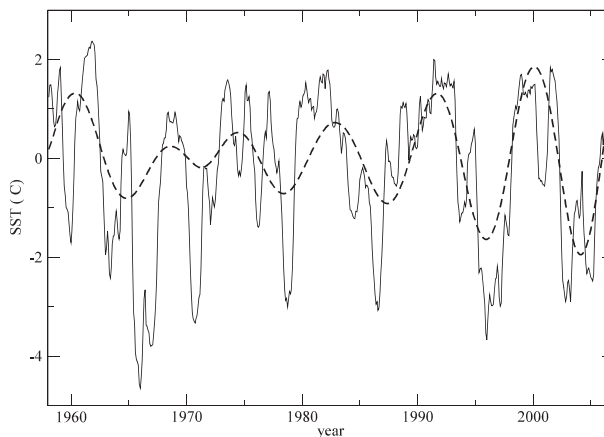


FIG. 6. Evolution of the reconstructed 8.5-yr oscillatory mode in SST at the point ( $37^{\circ}$ N,  $74^{\circ}$ W), where its amplitude in the CHR region is maximal; raw data shown as the solid line, and RCs (3, 4), which capture the oscillation, as the dashed line.

$74^{\circ}$ W) where it reaches its maximum amplitude. The 8.5-yr oscillation (dashed curve) captures quite well the interannual variability of the raw data (solid curve); its amplitude has increased markedly after about 1975.

Phase composites of this leading interannual mode are shown in Fig. 7, again by dividing the cycle into eight phase categories and plotting the first four. The mode consists of SST anomalies elongated along the axis of the mean Gulf Stream front (last panel). These features appear first just off the separation point at Cape Hatteras (first panel) and develop into a meander of the front with maximum amplitudes near  $73^{\circ}$  and  $66^{\circ}$ W.

The spatial patterns of the phase composites for the 5.2- and 3.8-yr oscillatory modes (not shown) are similar to those in Fig. 7. This similarity suggests the existence of a dominant spatial mode of variability of the front that tends to oscillate at discrete periods. The significant ST EOFs, ordered by decreasing variance, along with the associated periods and variances are the following: ST EOF 5 has a period of 6.2 yr and a variance of 4.3%; ST EOF pair (6, 7) has a period of 4.5 yr and a variance of 6%, but its amplitude increases by a factor of 2 after 1987 (not shown); and, finally, pair (8, 9) has a period of 3.7 yr and a variance of 5%.

To test the physical robustness of these interannual modes identified in the SST field, the analysis was repeated using the SSH field within the CHR region, using the same 12-month running mean prefiltering. The leading oscillatory mode again has a period of 8.5 yr and emerges in the ST EOF (3, 4) pair, which accounts for 12% of the interannual variance. The mode's spatio-temporal pattern, shown in Fig. 8 in terms of phase composites, approximately mirrors that seen in the SST field illustrated in Fig. 7.



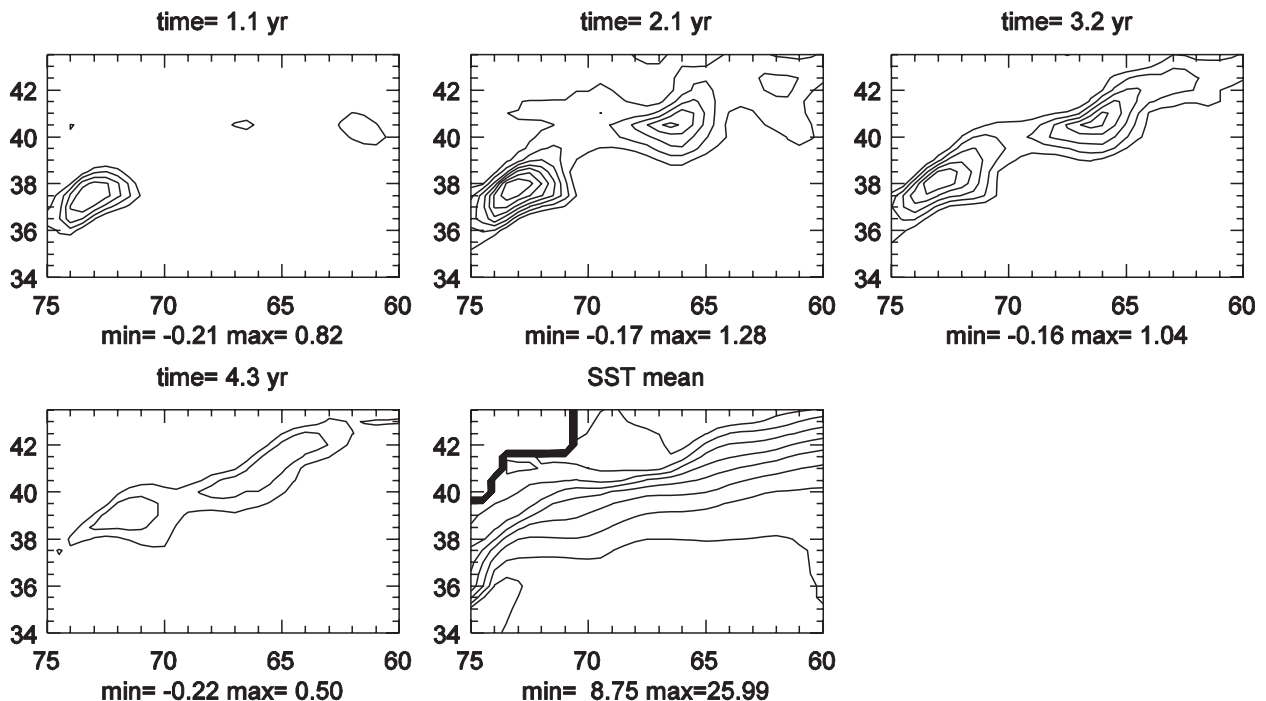


FIG. 7. Composites of the 8.5-yr mode of SST in the CHR region, in four phase categories, which correspond to the first half of the period. These composites are based on MSSA pair (3, 4), which captures 13% of the total variance (positive contours solid, negative ones dashed). Phase categories are labeled by their midpoint, as in Fig. 4, and CI = 0.15 K; the mean SST (bottom right panel) has CI = 1.7 K.

The spatiotemporal pattern of the 8.5-yr mode in SSTs and SSHs shares certain features with the so-called gyre mode that characterizes the interannual variability in the double-gyre problem of the midlatitude wind-driven ocean circulation (Jiang et al. 1995; Dijkstra and Ghil 2005). This gyre mode was found to have a dominant 7–8-yr peak across a hierarchy of ocean models: QG and shallow-water, barotropic and baroclinic (Speich et al. 1995; Ghil et al. 2002b; Simonnet and Dijkstra 2002; Simonnet et al. 2003a,b, 2005; Dijkstra and Ghil 2005). In particular, the gyre mode is known to propagate perpendicular to the direction of the midlatitude jet.

This propagation is quite obvious in the SST anomalies of Fig. 7: in the four composite phases labeled from 1.1 to 4.3 yr, the anomaly propagates from 36°–38°N to 38°–40°N; that is, it propagates in 3 years by ~150 km; this corresponds to a mean propagation speed of 50 km yr<sup>-1</sup>. In the SSH anomalies of Fig. 8, close examination of the four panels labeled 1.1 yr to 4.3 yr shows that—while there is no propagation of the anomaly features in their entirety—the northward expansion of the eddies might still be interpreted as northward propagation of the mean location of the features.

The other significant oscillatory modes in the SSH field also coincide roughly with those found in the SST as follows: ST EOF 5 has a period of 6.6 yr and a variance of 4.2%; the triad (6, 7, 8) has a period of 3.7 yr and

variance of 9%; and ST EOF 9 has a period of 4.2 yr and variance of 2.7%. The phase composites of these significant oscillatory modes again have spatiotemporal patterns similar to those of the 8.5-yr mode.

To analyze the SST evolution in the GBR rectangle (42°–50°N, 55°–35°W), we first removed the long-term trend, as captured by RCs (1, 2) of the MSSA analysis with a 150-month window; although the trend was not important in the CHR region and so it did not need to be subtracted from the raw data there, it accounts here for 18% of the total variance. After removing it, we applied MSSA again to the detrended time series with  $M = 150$  months.

The MC MSSA spectrum is shown in Fig. 9. The leading oscillatory mode is captured by ST EOFs (1, 2), has a period of 10.5 yr, and accounts for 10% of the total variance of the series, including the trend. This oscillatory mode is shown in Fig. 10 at the point (44°N, 47°W) where it reaches its maximum amplitude within the GBR region.

Phase composites of the 10.5-yr mode in eight phases are shown in Fig. 11. The anomalies are most prominent just eastward of the point where the mean SST front starts to diverge, near 50°W; they are broader scale and noisier than in the CHR region. The oscillatory mode's spatiotemporal evolution suggests an extension-and-contraction of the subpolar gyre. The other significant

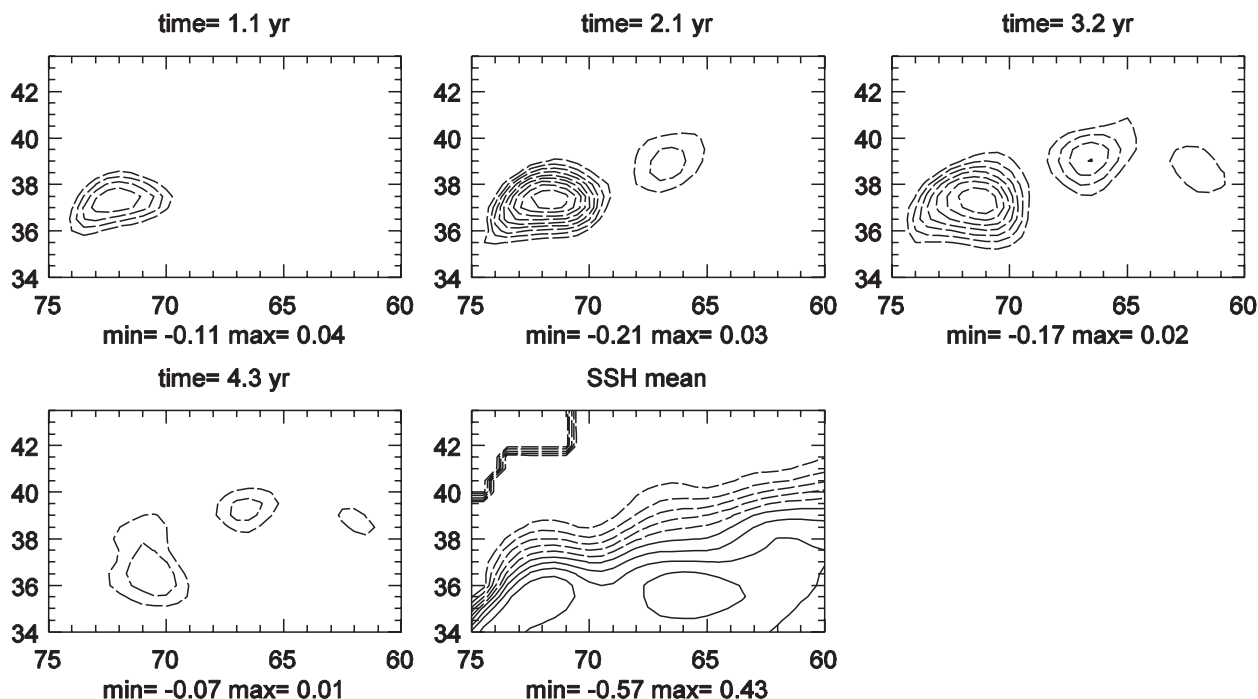


FIG. 8. As in Fig. 7, but of SSH: the four phase composites capture 12% of the total variance; CI = 0.02 m, while CI = 0.13 m for the mean SSH field.

oscillatory modes in the SST field are the following: the pair (3, 4) has a period of 5.7 yr and captures a variance of 8%, while the pair (6, 7) has a period of 3.2 yr and a variance of 5%. Taken together, these three modes—10.5, 5.7, and 3.2 yr—account for 23% of the total variance of the time series, including the trend. The phase composites of these significant oscillatory modes resemble those of the 10.5-yr oscillatory mode in Fig. 11. It seems therefore that, as in the CHR region, a single spatiotemporal mode dominates the interannual variability but with periods that differ somewhat from those seen in the other region.

Several differences between the flow of the Gulf Stream in the CHR and GBR regions are described below: they are largely due to the very different nature of the bottom topography and have been investigated over the years in some detail. The North Atlantic western boundary current, after leaving the Straits of Florida, flows over the shallow continental shelf, where water depth does not exceed 1000 m, and separates from the U.S. East Coast at Cape Hatteras by crossing the continental rise, where the bottom topography drops sharply to 5000 m within a few hundred kilometers (Özgökmen et al. 1997).

As the Gulf Stream approaches the Grand Banks, the mass transport by the Gulf Stream decreases, as some of the water is recirculated to the west, some of it continues to the east and crosses the Mid-Atlantic Ridge in the

Azores Current, and the remainder forms the North Atlantic Current (NAC) that continues as a well-defined boundary current along the eastern slope of the Grand Banks. At about 51°N the NAC moves to the east. As the waters flow eastward, the NAC loses its structure as a well-defined jet and the water is transported eastward in the subpolar front, which is the boundary between the warm water in the subtropical gyre and the cooler and less saline water in the subpolar gyre to the north (Rossby 1999).

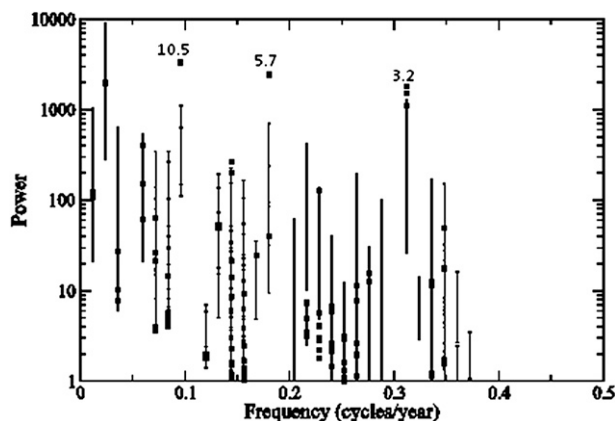


FIG. 9. Spectral analysis of the SST evolution in the GBR region (42°–50°N, 55°–35°W) after detrending and by using MC MSA with window width  $M = 150$  months. Same conventions as in Fig. 5; surrogate time series produced the same way as there.

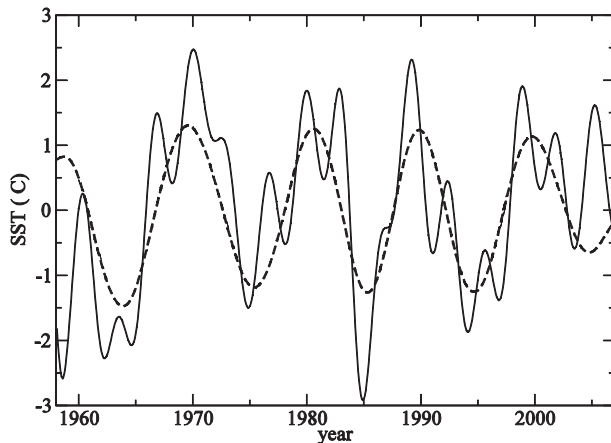


FIG. 10. Evolution of the reconstructed 10.5-yr oscillatory mode in SST at the point (44°N, 47°W) where its amplitude is maximal in the GBR region; raw data are shown as the solid line and RCs (1, 2), which capture the oscillation, as the dashed line.

These very different bathymetric and water-mass settings can help explain the slight differences between the oscillatory features illustrated in Figs. 5–8 for the CHR and Figs. 9–11 for the GBR. A more detailed study of the interannual variability in the two regions has to be left for subsequent work.

#### 4. Atmospheric model simulations

##### a. Instantaneous and mean fields

The coupled MABL–QG atmospheric model of Eq. (4) was integrated for 50 years beginning in January 1958. The only forcing of the model is the monthly mean

of  $\nabla^2 T$  as obtained from the SODA data. The initial streamfunction and vorticity were set to zero, and the spinup of the atmospheric circulation takes less than two months (see FGS07).

Daily snapshots are shown in Fig. 12 for the evolution of the streamfunction field: barotropic, baroclinic, near the surface, and at an altitude of 10 km, respectively. The barotropic streamfunction (upper row of three panels) exhibits intervals during which the jet is both strong and long, such as at time = 1996.3; this occurs mainly during the winter when the SST front reaches its maximum strength. In this configuration, the simulated atmospheric jet has large meanders accompanied by cyclonic flow to the north and anticyclonic flow to the south. The length of the jet is more than 5000 km, and its speed reaches values of  $7 \text{ m s}^{-1}$ .

There are also time intervals during which the jet practically disappears, such as at time 1993.8; this occurs mainly during the summer when the SST front reaches its minimum strength. Transitions between the two extreme states are illustrated here at time = 2007.3. Snapshots of the baroclinic streamfunction taken at the same times (second row in Fig. 12) show that there are intervals during which strong baroclinic eddies accompany the strong jet, such as at time = 1996.3, while the weak jet intervals tend to be accompanied by very weak eddy activity, such as at time = 1993.8. These atmospheric circulation patterns show similarities with those found in FGS04 and FGS07 when using idealized SST fronts. The zonal wavelength of the baroclinic eddies in Fig. 12 is about  $20^\circ$  longitude or a zonal wavenumber 18.

The time-mean barotropic and baroclinic streamfunction fields calculated over the full 50 years of the

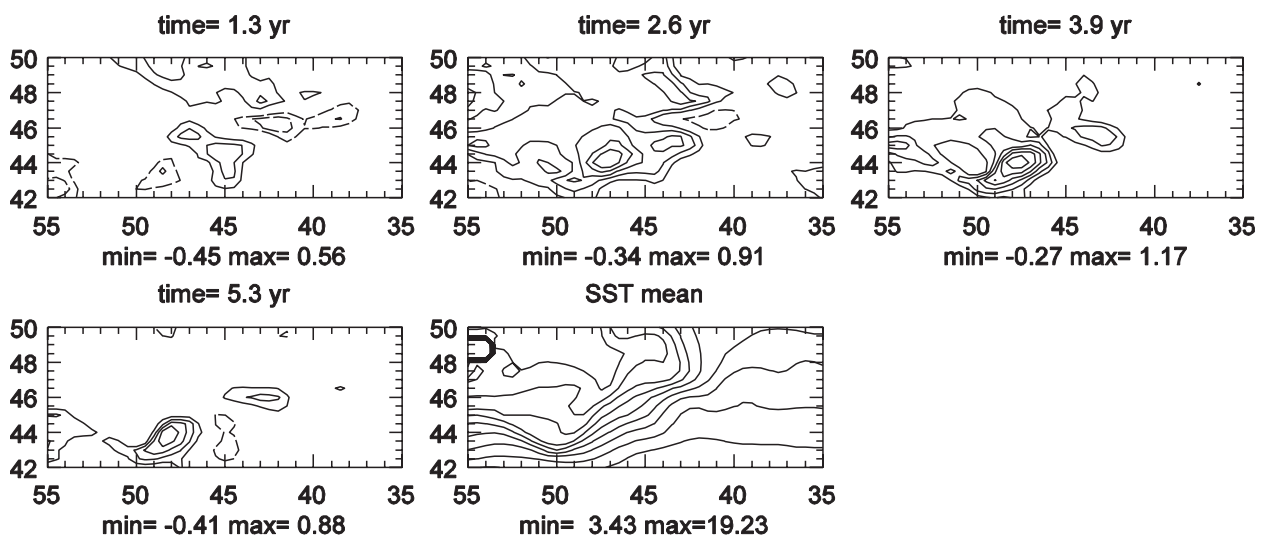


FIG. 11. As in Fig. 7, but of the 10.5-yr mode of SST in the GBR region: the four phase composites, based on the MSSA pair (1, 2), capture 10% of the total variance; CI = 0.15 K, CI = 1.7 K for the mean SST field.

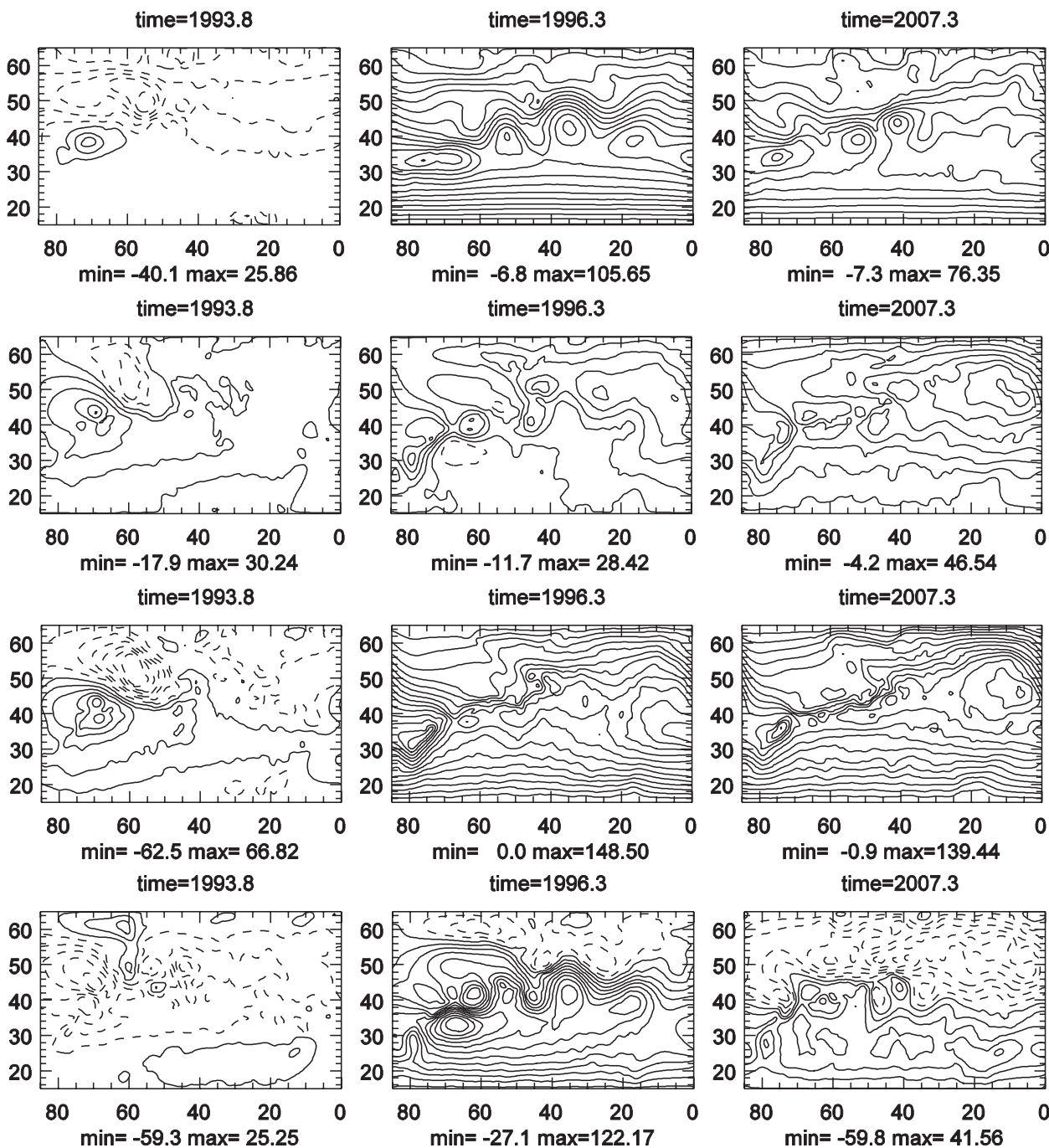


FIG. 12. Evolution of the atmospheric jet induced by the SODA history of the SST field in the coupled MABL–QG model of FGS07. Snapshots are shown at unequally spaced times, with the time, as well as the maximum and minimum values, given in the legend of each plot. Positive (negative) contours are solid (dashed): (top) barotropic component, CI = 8; (second row) baroclinic component, CI = 6; (third row) surface streamfunction, CI = 10; (bottom) streamfunction at an altitude of 10 km, CI = 10. CIs are in nondimensional units.

simulation are shown in the last panels of Figs. 14 and 15, respectively, in section 4c below. The mean barotropic jet is strongest between 60° and 40°W and tends to coincide with the GBR region in which the SST front diverges.

Daily snapshots of the surface streamfunction evolution are shown in the third row of Fig. 12. There is a jet roughly between 70° and 40°W, just over the Gulf Stream front, and a cyclonic eddy in the western part of the domain. The surface jet has its episodes of the weak

and short jet as at time = 1993.8 and of the strongest and longest jet at time = 1996.3, like the barotropic mode. The length of the surface jet reaches 3000 km, much shorter than in the barotropic component and at the altitude of 10 km (see below). This difference is due to the different effects of the two mechanisms that spin up the jet, as discussed in section 2b.

Daily snapshots of the streamfunction evolution at an altitude of 10 km are shown in the bottom row of Fig. 12. The spatial patterns are very similar to those of the barotropic component, but the jet and eddies are much stronger in the western part of the domain. This effect is due to the baroclinic component that gives rise to the baroclinic instability shown in the second row, and to the formation of eddies. The jet speed at 10 km reaches values of  $18 \text{ m s}^{-1}$ , and its length is up to 5000 km during the intervals of most vigorous flow. Easterlies appear in the model simulation south of  $30^\circ\text{N}$ .

The limit to the length of zonal jets follows from the theory of geostrophic turbulence (Charney 1971) in the presence of the  $\beta$  effect (Rhines 1975; Salmon 1998, section 6.3) and describes, in particular, the effect of localized midlatitude stirring of an initially quiescent flow in a periodic  $\beta$  channel. In our case, the localized stirring is provided by the finite-length, southwest–northeast oriented SST front. Considerations of energy and potential enstrophy conservation predict that the resulting flow is strongly eastward near the latitude of the stirring and weakly westward everywhere else; see Eq. (6.3.19) and Fig. 6.4 in Salmon (1998). FGS04 found that the jet length in their simulations and the theoretical formula agree quite well (see their Table 2).

### b. Spectral analysis

To focus on interannual oscillations, periods shorter than or equal to 1 yr were again removed by applying a 12-month running average to the model simulations. MSSA was then applied to the filtered data with a window width  $M = 150$  months. As for the SODA dataset, only those signals significant at the 95% level will be analyzed further below. We will analyze here the barotropic and baroclinic components as well as the surface streamfunction.

We first applied MC MSSA with a window of  $M = 150$  months to the barotropic and baroclinic components together; the resulting MC MSSA spectrum is shown in Fig. 13. The first two ST EOFs are associated with a nonlinear trend and have a variance of 23% (not shown). The leading oscillatory mode is captured by ST EOFs (3, 4); it accounts for a variance of 15% and has a nominal period of 8.2 yr. However, examination of the maximum entropy spectrum (Childers 1978; Penland et al. 1991; Ghil et al. 2002a) of the leading PCs obtained

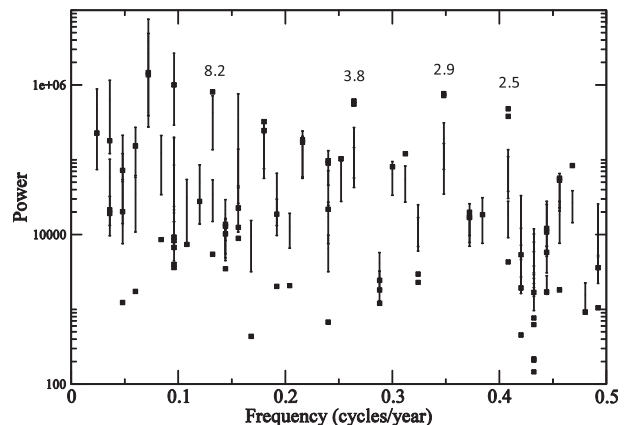


FIG. 13. Spectral analysis of the atmospheric model's combined barotropic and baroclinic modes using MSSA. The MC MSSA spectrum shown is computed with window width  $M = 150$  months; other details as in Figs. 5 and 9.

by a conventional EOF analysis of the same fields (not shown) reveals a broad peak in the 7.8–10-yr band. This broad peak brackets the 8.5-yr and 10.5-yr oscillations identified in the SST field in the CHR (Fig. 7) and GBR (Fig. 11) regions, respectively, and might be interpreted as an integrated atmospheric response to them. In section 5 below, we show that this atmospheric peak disappears from the model circulation when we filter out these two SST oscillations from the SODA dataset.

Phase composites of the RCs of the 7.8–10-yr mode in the first half of the period are shown in Figs. 14–16a for the barotropic, baroclinic, and surface streamfunctions, respectively; the counterparts of these phase composites at 10-km altitude (not shown) resemble the barotropic ones in Fig. 14. The anomalies in the barotropic mode exhibit an intense jet during the phases labeled “time = 2.0 yr” and “time = 3.1 yr” over the CHR and GBR regions (cf. Fig. 1), where the Gulf Stream is most variable and intense, and they are substantial over the whole domain. South of  $30^\circ\text{N}$ , the flow in the anomaly changes to a westward direction and might explain the westward propagation of this mode around the globe as a broad jet whose intensity oscillates in time. Feliks et al. (2010a), for instance, found oscillations with a period of 7–8 yr over the Eastern Mediterranean and even the Ethiopian Plateau.

In the baroclinic mode (Fig. 15), the largest amplitudes are present at the same time as in the barotropic mode. Moreover, a strong anticyclonic eddy is found in the western part of the domain, and a large, but weak, cyclonic gyre covers the rest of the domain. This gyre has a weak eastward flow in its southern part, between latitudes  $15^\circ$  and  $25^\circ\text{N}$ , and westward flow in its northern part, between  $35^\circ$  and  $50^\circ\text{N}$ .



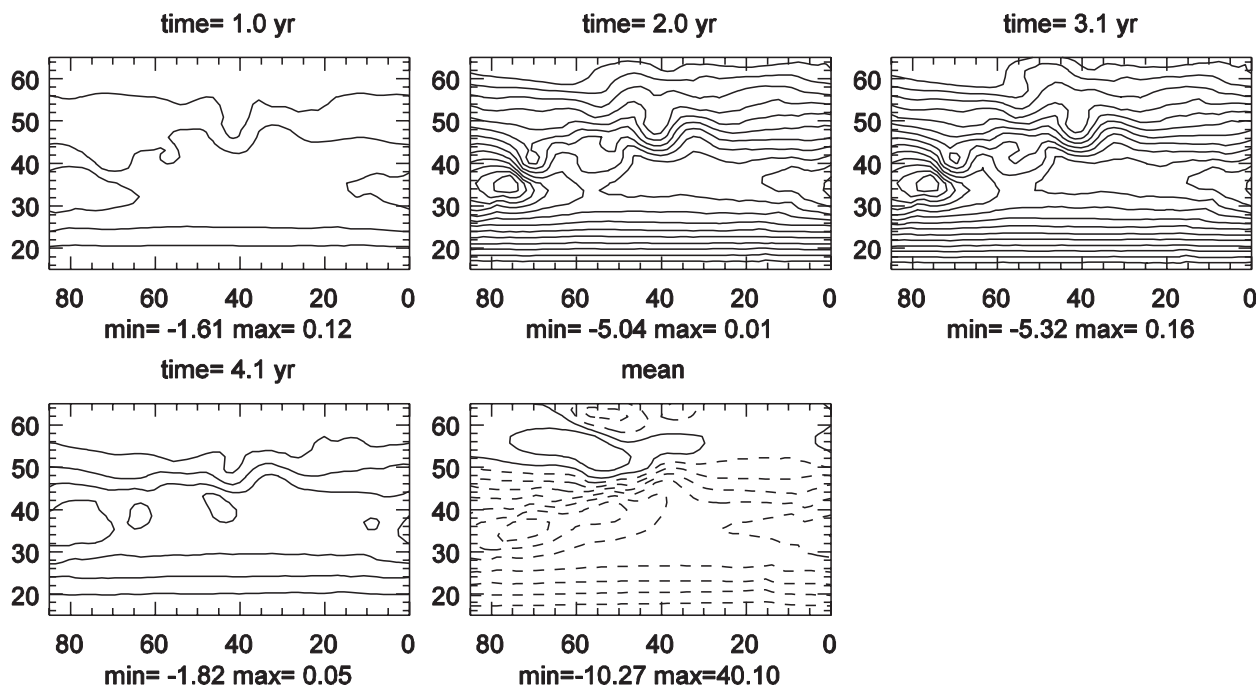


FIG. 14. Composites of the 7.8–10-yr mode of the atmospheric model's barotropic component, in four phase categories, like for the oceanic composites in Figs. 4, 7, 8, and 11. These composites are based on the MSSA pair (3, 4), which captures 15% of the total variance; here,  $CI = 0.25$ . Note that this broad peak in the atmospheric model encompasses the narrower oceanic peaks at 8.5 and 10.5 yr in the CHR and GBR regions, respectively; see Figs. 5 and 9. The mean field (last panel) has  $CI = 4.9$  (nondimensional units).

In the sensitivity experiment in which the width of the sponge layer was  $\Delta L = 750$  km, no significant differences between this solution and the one with  $\Delta L = 1000$  km were found. In the second experiment, with  $\Delta L = 500$  km, the solution became unstable after 35 years. The analysis was carried out over these 35 years, and the main features in the mean circulation and in the interannual oscillatory modes, like those appearing in Fig. 15 near the western boundary, look very similar to those for  $\Delta L = 1000$  km or  $\Delta L = 750$  km, although the 8.5-year mode had less than four full cycles. We thus conclude that the width  $\Delta L$  of the sponge layer has little effect on the main spatiotemporal features of the solution, but is quite important in maintaining its stability.

The seasonal cycle mode near the surface is shown in Fig. 16b. In the summer, the seasonal cycle anomaly reduces the mean flow, which is therefore weak on average. In the winter, the seasonal cycle anomaly enhances the mean flow, which is therefore strong in this season. The amplitude of the seasonal mode is larger by an order of magnitude than the amplitude of the 7.5–10-yr mode, and the snapshots shown in Fig. 12 are, therefore, mainly influenced by the seasonal cycle. While the interannual modes have a smaller direct influence on the large-scale atmospheric flow than the march of the seasons, their effect on weather variability from year to year can still

be significant, as suggested by the documented impact of the NAO phase on weather phenomena near and far from the North Atlantic (Hurrell et al. 2003; Feliks et al. 2010a).

The other significant ST EOFs, ordered by decreasing variance, along with the associated periods and variances are the following: ST EOFs (5, 6) have a dominant period of 2.9 yr and a variance of 12%; ST EOFs (7, 8) have a dominant period of 3.8 yr and a variance of 9%; ST EOFs (9, 10) have a dominant period of 2.5 yr and a variance of 7%. The phase composites of these oscillatory modes have spatial patterns that resemble those of the 7.8–10-yr mode but with smaller amplitude. The similarity of the spatial patterns of the four statistically significant atmospheric oscillatory modes with different periods is consistent with the similar structure of the oscillatory modes in the SST fields.

### c. Comparison with the observed NAO index

The central hypothesis of this paper is that the interannual oscillations found in observed atmospheric data over the North Atlantic are spun up by interannual oscillations of the Gulf Stream front. To further support the results reported above, we next compare the oscillations found in our atmospheric model simulations with an analysis of the observed NAO index.

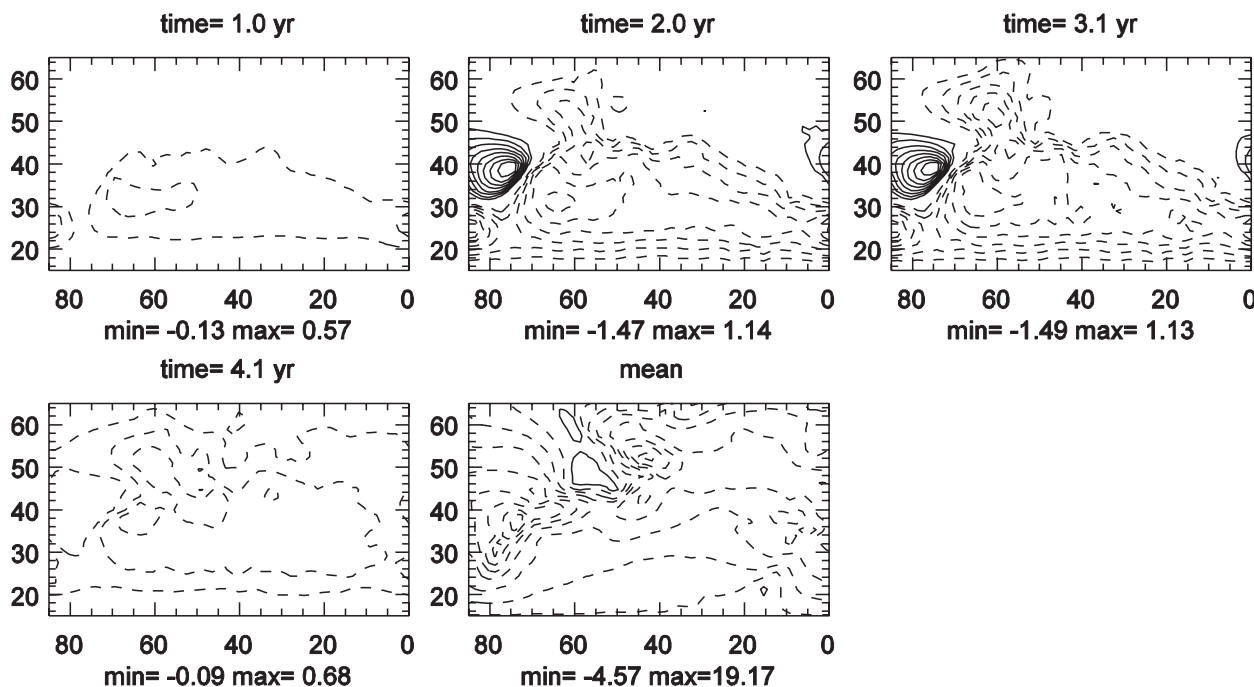


FIG. 15. As in Fig. 14, but for the baroclinic component: CI = 0.15 for the four composites; CI = 2.3 for the mean.

The NAO has been studied extensively over the last two decades (Hurrell et al. 2003), and its strength has been quantified using several indices. We use here the monthly index over the years 1823–2007, as compiled by Jones et al. (1997); the later, updated version is available online (at [http://www.cru.uea.ac.uk/~timo/projpages/nao\\_update.htm](http://www.cru.uea.ac.uk/~timo/projpages/nao_update.htm)). This index is defined by the difference between the normalized sea level pressure at Ponta Delgada, Azores, Portugal (37.7°N, 25.7°W), and the normalized sea level pressure over Iceland (65.7°N, 18.1°W).

Applying SSA to this index, Feliks et al. (2010a) identified significant oscillatory modes with periods of 7.7, 5.5, 4.0, 3.2, and 2.2 yr. Rogers (1984), Hurrell and van Loon (1997), Robertson (2001), Gámiz-Fortis et al. (2002), and Paluš and Novotná (2004) also found an oscillation with a period of  $\sim 8$  yr in the NAO index. A quasi-biennial component is present in the closely related Arctic Oscillation, constructed from hemispheric sea level pressures, as well (Trenberth and Paolino 1981; Robertson 2001).

We compare here the observed NAO index to its counterpart in the atmospheric model simulations, defined as follows. First we compute the model's surface pressure, equivalent to the streamfunction at the surface level,  $z = 0$ . The simulated NAO index (SNI) is then defined to be the difference in the model's surface pressure anomalies—that is, the deviation from the 50-yr mean of the simulation—between the points 41°N, 27°W and 59°N, 29°W; these two points are shown in Fig. 16 as points B and A. For these two model points,

the correlation between the SNI and observed NAO index is 0.52, that is, very close to the maximum value obtained when defining the model's SNI as the difference between any two points in the domain; the longitude of point A defining the SNI is located about 10 degrees west of the northern point defining the NAO index. This difference is due to the geometric distortion by the  $\beta$  plane used in the atmospheric model: longitude 29°W on the  $\beta$  plane at latitude 59°N corresponds to a longitude of 19°W on the globe; that is, point A does lie inside the model's Iceland.

In the following analysis, we again first filtered out the variability associated with periods shorter than or equal to 1 yr by applying a 12-month running average to each time series (Fig. 17a). We then applied a bivariate MSSA to the NAO index (channel 1) and to the SNI index (channel 2), with a window width of  $M = 200$  months, normalizing each index by its respective variance. ST EOF pair (3, 4) captures the lowest-frequency components, including the nonlinear trend (Ghil et al. 2002a), in both indices. To isolate any underlying low-frequency oscillations, we applied MSSA to the detrended indices with the same window width.

The MC MSSA spectrum is shown in Fig. 18, and only those signals that are significant at the indicated (two-sided) 95% level will be analyzed further below. The RCs corresponding to the three significant ST EOF pairs, ordered by decreasing variance, along with the associated periods and variances are shown in Fig. 17. These three

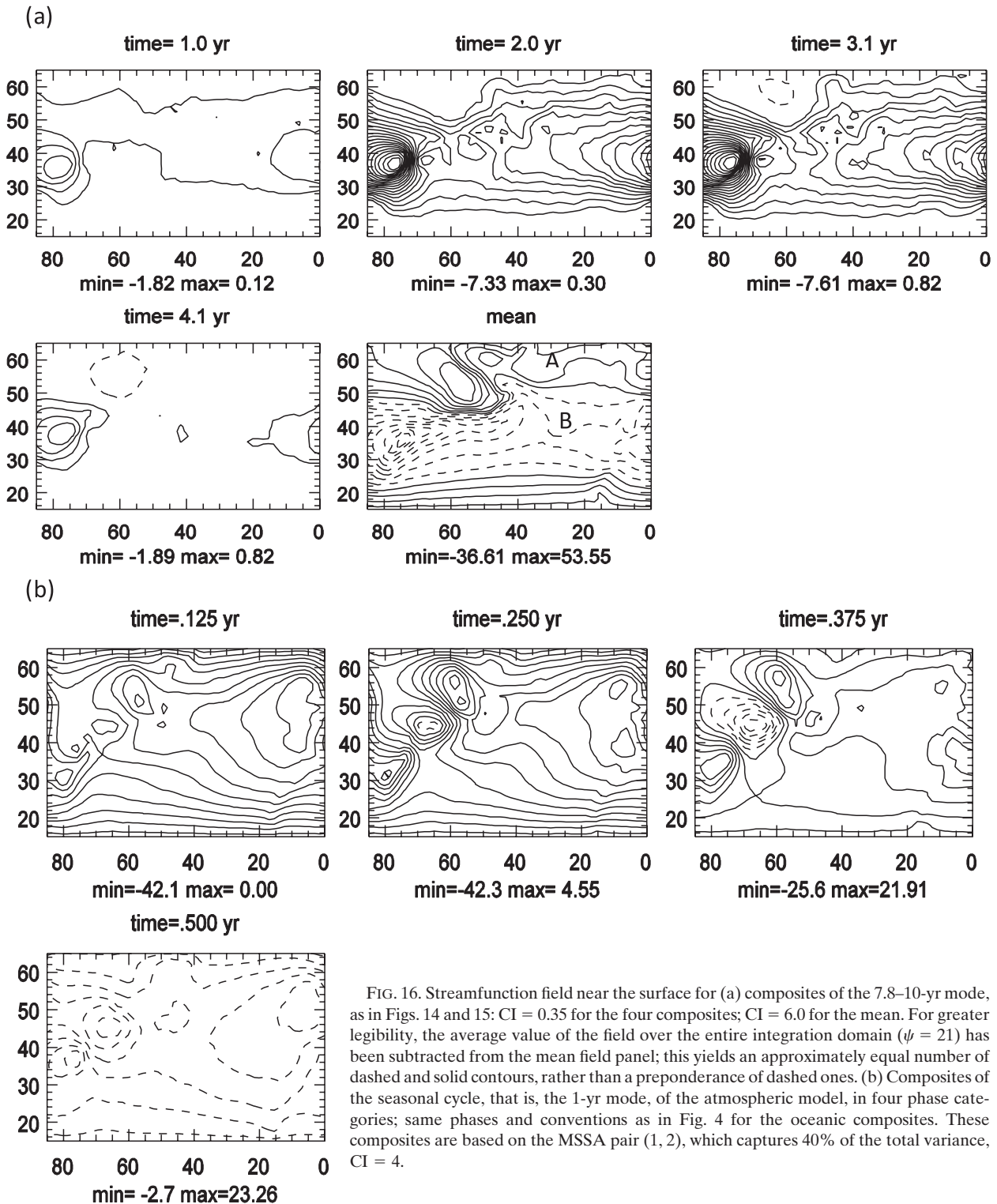


FIG. 16. Streamfunction field near the surface for (a) composites of the 7.8–10-yr mode, as in Figs. 14 and 15: CI = 0.35 for the four composites; CI = 6.0 for the mean. For greater legibility, the average value of the field over the entire integration domain ( $\psi = 21$ ) has been subtracted from the mean field panel; this yields an approximately equal number of dashed and solid contours, rather than a preponderance of dashed ones. (b) Composites of the seasonal cycle, that is, the 1-yr mode, of the atmospheric model, in four phase categories; same phases and conventions as in Fig. 4 for the oceanic composites. These composites are based on the MSSA pair (1, 2), which captures 40% of the total variance, CI = 4.

modes of covariability between the observed and simulated indices capture 60% of the covariance and show high visual similarity between the observed NAO index and the SNI on these time scales.

We analyzed these three oscillatory modes further to quantify their degree of synchronization, following Feliks et al. (2010a). For each oscillatory mode, this analysis measures the correlation of the amplitude

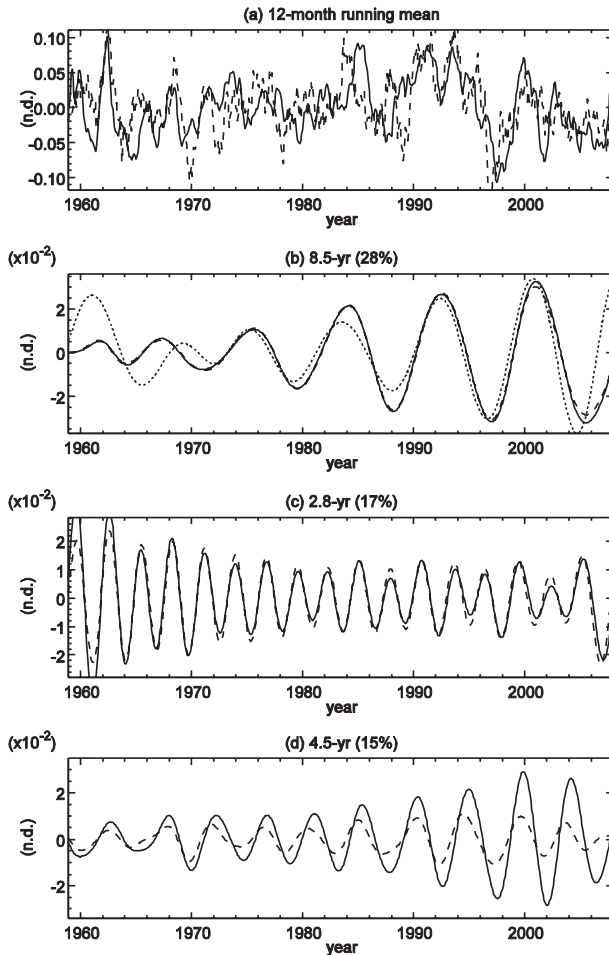


FIG. 17. The observed NAO index (dashed line) and SNI (solid line): (a) 12-month running mean, and (b)–(d) the RCs of the significant oscillatory modes in both the observed and simulated NAO indices, ordered by decreasing variance, along with the associated periods and variances. The dotted line in (b) is the reconstructed 8.5-yr oscillatory mode in the SST at the point ( $37^{\circ}\text{N}$ ,  $74^{\circ}\text{W}$ ) that was shown already in Fig. 6; it is divided here by 45.6 for proper scaling to the nondimensional RCs.

modulation between the observed NAO index and the SNI, the degree of phase synchronization, and the ratio  $\varepsilon$  of the energy that is contained in each of the two indices,  $\varepsilon = E(\text{RC}_{\text{SNI}})/E(\text{RC}_{\text{NAO}})$ ; the energy  $E$  of a pair of RCs is simply defined as the corresponding variance.

For the 8.5-yr oscillatory mode, there is *complete* synchronization of frequency, phase, and amplitude between the observed NAO index and the SNI—that is, in the terminology of Feliks et al. (2010a), the synchronization level is FPA: the correlation  $r$  between their modulated amplitudes is of  $r = 0.99$ ; the difference  $\sigma$  between their phases,  $\sigma = 0.11$  rad, is very small; and their energies are also very similar, with a ratio of  $\varepsilon = 1.08$ . The synchronization of the 2.8-yr mode is also of type FPA with

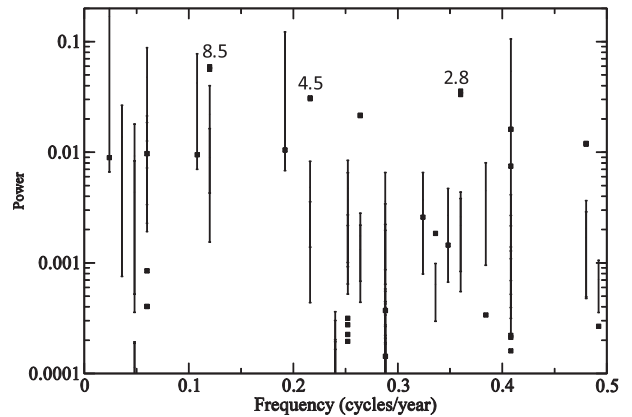


FIG. 18. Spectral analysis of the observed NAO index and the atmospheric model's SNI, obtained by MC MSA with window width  $M = 200$  months; other details as in Fig. 9.

$r = 0.91$ ,  $\sigma = 0.19$  rad, and an energy ratio of  $\varepsilon = 1.15$ . The 4.5-yr mode is *marginally* synchronized in frequency and phase—that is, of FP type following Feliks et al. (2010a), with  $r = 0.87$  and  $\sigma = 0.72$ , while the energy in SNI is significantly larger than in the observed NAO index  $\varepsilon = 5.6$ .

The above synchronization analysis provides further quantitative evidence of the high degree of similarity between the interannual modes of the observed NAO index and the SNI—and, by inference, for the role of the Gulf Stream front in driving these oscillations in the observed NAO. The direct connection between the 8.5-yr oscillatory mode in the SST field of the SODA reanalysis and that of the observed NAO index is shown in Fig. 17b. In this panel, the 8.5-yr mode in SST is plotted (dotted line) at the point ( $37^{\circ}\text{N}$ ,  $74^{\circ}\text{W}$ ) where this anomaly reaches its maximum amplitude; this mode is also shown in Fig. 6 (dashed line there). There is a particularly good fit for 1972–2002; the divergence after that is probably due to an edge effect since in dimensional units  $M = 16.7$  yr. The correlation between SNI and SST in their amplitude modulation is  $r = 0.79$ .

#### d. The atmospheric circulation for spatially and temporally smoothed SST fields

In the previous sections, we have made the case that the interannual oscillations in the observed NAO index can be attributed to similar oscillations found in the Gulf Stream front. It might be countered that this is merely an association and that our atmospheric model is responding, in fact, to large-scale SST variability imprinted in the SODA dataset by the history of the atmospheric circulation's variability over the North Atlantic. We provide further evidence in this subsection that the Gulf Stream front does play a key role in driving the

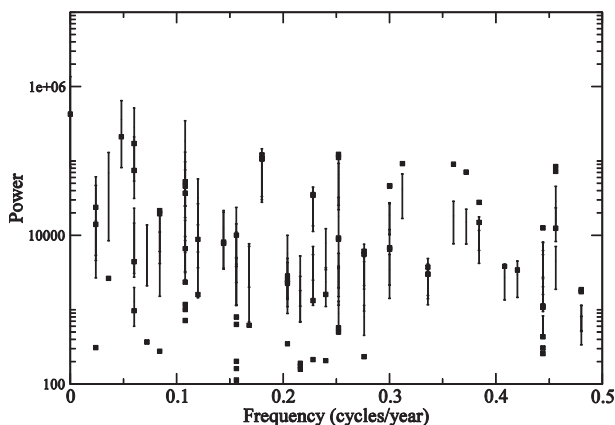


FIG. 19. As in Fig. 13 but when the atmospheric model is driven by a flat SST field, with  $\nabla^2 T = 0$ , in the domain ( $32^\circ$ – $50^\circ$ N,  $85^\circ$ – $40^\circ$ W): MC MSA spectrum computed with window width  $M = 150$  months, same conventions as in Figs. 9 and 13.

variability of the atmospheric circulation. To do so, we reran the MABL–QG model with  $\nabla^2 T = 0$  in the spherical rectangle ( $32^\circ$ – $50^\circ$ N,  $85^\circ$ – $40^\circ$ W), which includes both CHR and GBR regions of the front (see again the boxes in Fig. 1). In this simulation, therefore, the Gulf Stream front cannot impact the model atmosphere, whose forcing derives only from the surrounding regions.

The atmospheric circulation in this experiment changes drastically: both the jet and its associate eddies disappear completely. Repeating the MSA analysis of section 4b, there were no statistically significant oscillations in the 7.8–10-yr range; there are some statistically significant higher frequency oscillations (Fig. 19), but none has a period longer than 3 yr and their energy is smaller by an order of magnitude than in the control experiment (Fig. 13).

In the next experiment, we spatially smoothed the oceanic SST front to be similar to those used by typical GCMs by filtering out wavelengths shorter than 400 km. We forced the atmospheric model with the smoothed SST field. Snapshots of the atmospheric circulation so obtained are shown in Fig. 20; they are much weaker and miss entirely the strong jet and eddies when compared to the control experiment, as shown in Fig. 12. In fact, unlike in Fig. 12, there is barely a difference between the weakest jet (time = 1993.8) and the strongest one (time = 1996.3). The MSA analysis was not able to identify statistically significant oscillations in the 7.8–10-yr range, although here, too, there are some statistically significant higher-frequency oscillations (Fig. 21) whose energy is smaller by an order of magnitude than in Fig. 13.

In yet another experiment, we forced the model atmosphere over the entire domain of Fig. 1 but with the SST variability low-pass filtered in time so that no periods longer than 2 yr were present: note that the time-mean SST was included in the forcing. Snapshots of the atmospheric circulation in this integration (not shown) were found to be very similar to those obtained in the control run, with the mean fields also being very similar to those shown in Figs. 14–16 (last panels). In contrast to the control experiment, though, the MSA analysis was not able to identify statistically significant oscillations in the 7.8–10-yr range (Fig. 22). As in Figs. 5, 13, and 21, there is a statistically significant peak at 3.8 yr, as well as some higher-frequency oscillations, but their energy is again smaller by an order of magnitude than in the control experiment (Fig. 13).

From these three experiments we conclude that, when the SST field is either spatially smoothed or the 7.8–10-yr peak is removed from it, then the 7.8–10-yr oscillations are also eliminated from the atmospheric circulation.

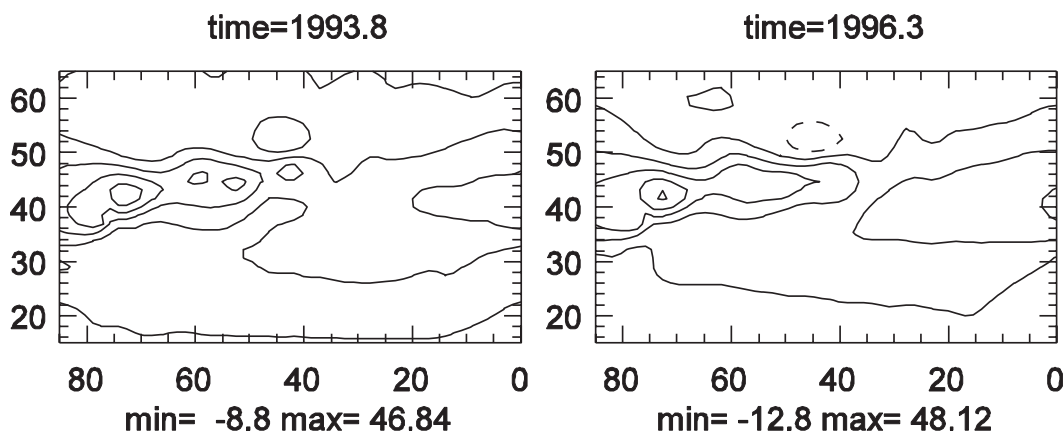


FIG. 20. Evolution of the atmospheric streamfunction at altitude 10 km but when the model is driven by a spatially smoothed SST field; see text for details. The two snapshots are shown at the times of weakest and strongest jet respectively, CI and other conventions as in the lowermost row of Fig. 12.



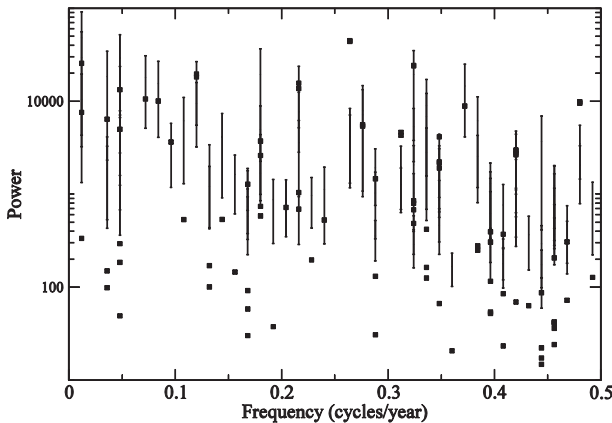


FIG. 21. Spectral analysis of the atmospheric model's combined barotropic and baroclinic modes, but when the model is driven by a spatially smoothed SST field; see text for details. MC MSSA spectrum computed with window width  $M = 150$  months, same conventions as in Figs. 9 and 13.

It follows that we can indeed attribute the 7.8–10-yr oscillations in the atmosphere to similar oscillations in the SST front.

## 5. Concluding remarks

### a. Summary

The cause of interannual oscillations in the extratropical atmosphere is a matter of long-standing argument. There is substantial consensus on the extratropical effects of ENSO, but these do not extend to periods longer than 4–5 yr. Several theories exist for the well-known 7–8-yr peak in the NAO (e.g., Deser and Blackmon 1993; Dettinger et al. 1995; Plaut and Vautard 1994; Moron et al. 1998; Wunsch 1999; Da Costa and Colin de Verdière 2002; Hurrell et al. 2003; Felix et al. 2010a), and they were briefly summarized in the introduction. In this paper, we showed that sharp SST fronts associated with the Gulf Stream can spin up an atmospheric jet over the North Atlantic and give rise to oscillations with such a period in a simplified atmospheric model.

First, we analyzed in section 3 monthly SST and SSH fields, from the 50 years (1958–2007) of the SODA reanalysis dataset, over the North Atlantic region shown in Fig. 1. We found two regions along the Gulf Stream front that have prominent and statistically significant narrow-band interannual oscillations—namely, the region just downstream of Cape Hatteras (CHR) and in the Grand Banks region (GBR), centered at 44°N, 47°W. Several statistically significant oscillatory modes were found in these two regions: their periods include an 8.5-yr mode in the CHR region and a 10.5-yr mode in the GBR region (Figs. 5 and 9, respectively).

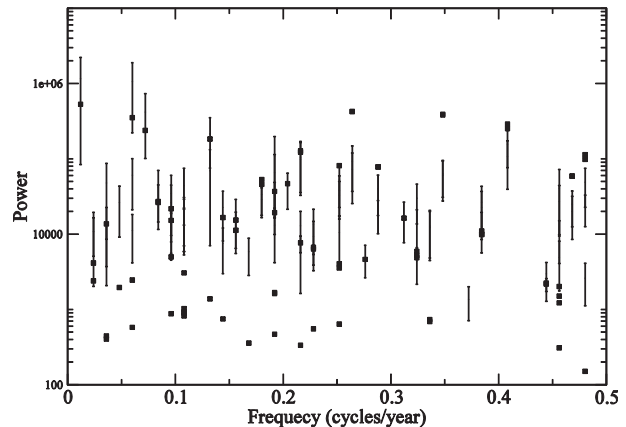


FIG. 22. As in Fig. 21, but as induced by the SST history from SODA and filtering out periods longer than 2 yr.

The spatiotemporal pattern of the 8.5-yr mode in both the SST and SSH fields within the CHR region (Figs. 7 and 8, respectively) shares certain features with the so-called gyre mode that characterizes the interannual variability in the double-gyre problem of the midlatitude wind-driven ocean circulation (Jiang et al. 1995; Dijkstra and Ghil 2005). This gyre mode was found to have a dominant 7–8-yr peak across a hierarchy of ocean models, QG and shallow-water, barotropic, and baroclinic (Speich et al. 1995; Ghil et al. 2002b; Simonnet and Dijkstra 2002; Simonnet et al. 2003a,b, 2005; Dijkstra and Ghil 2005).

Shorter-period SST oscillations were also identified with periods of 3.7, 4.5, and 6.2 yr in the CHR region and with 3.2-yr and 5.7-yr periods in the GBR region. The spatial patterns of all of these oscillatory modes include a large-scale Gulf Stream meander off Cape Hatteras, as well as extension and contraction of the jetlike feature in the GBR region. These two basic spatiotemporal patterns characterize all of the significant oscillations identified in the respective regions.

This similarity might seem surprising, given the fact that—in the free oscillations of a vibrating string or drumhead—higher-frequency oscillations are typically associated with smaller spatial scales. The difference is due to the fact that these oscillations in the western North Atlantic are strongly constrained by the bathymetry, on the one hand, and the prevailing wind pattern, on the other. The latter, of course, is affected in turn by the oceanic variability, as we have seen in section 4.

Following upon the results of FGS04 and FGS07, we used in section 4 the SST monthly history from the SODA dataset to drive the atmospheric model of FGS07 through the Laplacian of the SST field; compare to Eq. (3). In the resulting atmospheric simulations, in which  $\nabla^2 T$  was the sole model forcing, we identified two extreme states consisting of (i) an extended, strong jet state

and (ii) a state of very weak atmospheric flow with no jet, respectively (Fig. 12). In the former, a strong jet develops over the oceanic SST front, in which the jet extends farther eastward and reaches a length of 5000 km and a speed of  $18 \text{ m s}^{-1}$ . This jet is most prominent in the model's upper layer.

Prominent interannual oscillatory modes were found in the model atmosphere, with a spatial pattern characteristic of the strong jet state, with anticyclonic anomalies to the south of the jet and cyclonic ones to the north; both these features extend throughout the model's North Atlantic domain. The statistically significant oscillatory modes in the model's free atmosphere have periods of 7.8–10 yr, 3.8 yr and 2.9 yr (Fig. 13). This range of periods corresponds approximately to that of the oscillatory modes found in the SST front of the CHR and GBR regions, although the periods do not correspond exactly. The 7.8–10-yr mode in the model atmosphere is broad compared to the 8.5-yr and 10.5-yr modes identified in the SST front of the CHR and GBR regions, respectively, and may arise as a result of the nonlinear interaction between the two. Our results suggest that the spinup of the 3.8-yr mode may be induced by a more localized SST oscillation in the CHR region.

### b. Discussion

A striking result of this study is the close similarity between the observed NAO index and the model's simulated NAO index (SNI) [cf. section 4c (Fig. 17)]. Comparing the observed NAO index with the SNI, we found that the overall correlation is  $r = 0.52$ . The complete synchronization of the 8.5-yr oscillatory mode in the observed and simulated indices leads us to the conclusion that this NAO mode is induced by the mode with the same, or very similar, periodicity in the Gulf Stream front. This result is at least consistent with the review of Small et al. (2008) in which they emphasize that, in frontal zones and over eddies, it is indeed the ocean that drives the atmosphere, rather than the other way around (see also Manganello 2008).

The spatiotemporal pattern of the 8.5-yr mode in SSTs and SSHs shares certain features with the so-called gyre mode that characterizes the interannual variability in the double-gyre problem of the midlatitude wind-driven ocean circulation (Jiang et al. 1995; Simonnet and Dijkstra 2002; Simonnet et al. 2003a,b, 2005). This gyre mode was found to have a dominant 7–8-yr peak across a hierarchy of ocean models, QG and shallow-water, barotropic, and baroclinic (Speich et al. 1995; Chang et al. 2001; Ghil et al. 2002b; Dijkstra and Ghil 2005).

The gyre mode was shown to be robust with respect to forcing by the seasonal cycle in wind stress (Sushama et al. 2007) and had been found in a century of SST data

for the North Atlantic (Moron et al. 1998). Several other authors, going back to Veronis (1963, 1966), found intrinsic multimodality or interannual variability in the oceanic wind-driven circulation, even when the wind stress forcing is constant in time (Cessi and Ierley 1987; Meacham 2000; Nadiga and Luce 2001; Nauw and Dijkstra 2001); more complete references can be found in Dijkstra (2005) and Dijkstra and Ghil (2005). It would seem that the results of the present paper provide substantial evidence in support of such intrinsic ocean variability, in general, and the gyre mode, in particular, giving rise to near-decadal variability in the Gulf Stream, on the one hand, and in the NAO, on the other.

Further evidence that the 7–8-yr atmospheric mode is, indeed, induced by the near-decadal oscillations of the Gulf Stream front in the CHR and GBR regions is provided by three additional experiments. In these atmospheric model experiments, the SST front was (i) removed entirely, (ii) spatially smoothed, or (iii) low-pass filtered in time to remove the oscillations with periods longer than 3 yr. In all three cases, the 7–8-yr atmospheric mode disappeared, and other interannual oscillations were greatly attenuated.

If these findings are further confirmed by high-resolution GCM computations and observations—in the same way in which Minobe et al. (2008) confirmed those of FGS04 and FGS07—one could expect to find some predictive skill in the periodicity of the oceanic mode, first, and the atmospheric one thereafter. In FGS04 it was clearly shown that the imposed 7-yr periodicity in the SST front's strength resulted in substantial modulation of intraseasonal activity in the atmosphere above. Thus, one might be able to anticipate the frequency and severity of extreme events over Europe (e.g., Yiou and Nogaj 2004) from a monitoring of the Gulf Stream.

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